

**CENTRAL UNIVERSITY OF JHARKHAND**  
**DEPARTMENT OF MATHEMATICS**  
**2021 ONWARDS**

| <b>Programme structure for Two years M.Sc. degree programme in Mathematics</b> |             |                                               |   |   |   |           |
|--------------------------------------------------------------------------------|-------------|-----------------------------------------------|---|---|---|-----------|
| <b>L – Lecture, T- Tutorial, P – Practical (Lab), Cr – Credits.</b>            |             |                                               |   |   |   |           |
| <b>FIRST SEMESTER</b>                                                          |             |                                               |   |   |   |           |
| Sl. No.                                                                        | Course Code | Course Title                                  |   |   |   | CR        |
|                                                                                |             |                                               | L | T | P |           |
| 1.                                                                             | MMA 111020  | Differential Equations                        | 3 | 1 | 0 | 4         |
| 2.                                                                             | MMA 111031  | Mathematical Analysis                         | 3 | 1 | 0 | 4         |
| 3.                                                                             | MMA 111050  | Fundamentals of Computers and C Programming   | 2 | 0 | 2 | 4         |
| 4.                                                                             | MMA 111060  | Numerical Analysis                            | 3 | 1 | 0 | 4         |
| 5.                                                                             | MMA 111070  | Linear Algebra                                | 3 | 1 | 0 | 4         |
| <b>Total Credits</b>                                                           |             |                                               |   |   |   | <b>20</b> |
| <b>SECOND SEMESTER</b>                                                         |             |                                               |   |   |   |           |
| Sl. No.                                                                        | Course Code | Course Title                                  |   |   |   | CR        |
|                                                                                |             |                                               | L | T | P |           |
| 1                                                                              | MMA 121050  | Statistics – I                                | 3 | 1 | 0 | 4         |
| 2                                                                              | MMA 121060  | Complex Analysis                              | 3 | 1 | 0 | 4         |
| 3                                                                              | MMA121070   | Measure Theory and Integration                | 3 | 1 | 0 | 4         |
| 4                                                                              | MMA 121080  | Topology                                      | 3 | 1 | 0 | 4         |
| 5                                                                              | MMA 121090  | Abstract Algebra                              | 3 | 1 | 0 | 4         |
|                                                                                |             |                                               |   |   |   |           |
| <b>Total Credits</b>                                                           |             |                                               |   |   |   | <b>20</b> |
| <b>THIRD SEMESTER</b>                                                          |             |                                               |   |   |   |           |
| Sl. No.                                                                        | Course Code | Course Title                                  |   |   |   | CR        |
|                                                                                |             |                                               | L | T | P |           |
| 1                                                                              | MMA 211010  | Functional Analysis                           | 3 | 1 | 0 | 4         |
| 2                                                                              | MMA 211030  | Calculus of Variations and Integral Equations | 3 | 1 | 0 | 4         |
| 3                                                                              | MMA 211040  | Partial Differential Equations                |   |   |   |           |
| 4                                                                              |             | Elective – I                                  | 3 | 1 | 0 | 4         |
| 5                                                                              |             | Elective – II                                 | 3 | 1 | 0 | 4         |
| 6                                                                              | MMA 213060  | Seminar                                       |   |   |   | 2         |
| <b>Total Credits</b>                                                           |             |                                               |   |   |   | <b>22</b> |

| <b>FOURTH SEMESTER</b> |             |                         |   |   |   |    |
|------------------------|-------------|-------------------------|---|---|---|----|
| Sl. No.                | Course Code | Course Title            |   |   |   | CR |
|                        |             |                         | L | T | P |    |
| 1                      | MMA 221040  | Optimization Techniques | 3 | 0 | 1 | 4  |

| 2                                                    | MMA 221050  | Number Theory                                       | 3 | 1 | 0 | 4         |
|------------------------------------------------------|-------------|-----------------------------------------------------|---|---|---|-----------|
| 3                                                    |             | Elective – III                                      | 3 | 1 | 0 | 4         |
| 4                                                    | MMA 223030  | Project                                             |   |   |   | 6         |
| <b>Total Credits</b>                                 |             |                                                     |   |   |   | <b>20</b> |
| <b>List of Electives for 3<sup>rd</sup> Semester</b> |             |                                                     |   |   |   |           |
| Sl. No.                                              | Course Code | Course Title                                        |   |   |   | CR        |
|                                                      |             |                                                     | L | T | P |           |
| 1                                                    | MMA 215040  | Theory of Computations                              | 3 | 1 | 0 | 4         |
| 2                                                    | MMA 215060  | Field Theory                                        | 3 | 1 | 0 | 4         |
| 3                                                    | MMA 215070  | Statistics-II                                       | 3 | 1 | 0 | 4         |
| 4                                                    | MMA 215080  | Discrete Mathematics                                | 3 | 1 | 0 | 4         |
| 5                                                    | MMA 215090  | Fluid Dynamics                                      | 3 | 1 | 0 | 4         |
| 6                                                    | MMA 215100  | Theory and Applications of Fuzzy sets               | 3 | 1 | 0 | 4         |
| 7                                                    | MMA 215110  | Data Structures and Algorithm Analysis              | 3 | 0 | 1 | 4         |
| 8                                                    | MMA 215120  | Cryptography                                        | 3 | 1 | 0 | 4         |
| 9                                                    | MMA 215130  | Java Programming                                    | 3 | 0 | 1 | 4         |
| 10                                                   | MMA 215140  | Graph Theory                                        | 3 | 1 | 0 | 4         |
| 12                                                   | MMA 215150  | Mathematical Modelling                              | 3 | 1 | 0 | 4         |
| 13                                                   | MMA215160   | Integral Transforms                                 | 3 | 1 | 0 | 4         |
| 14                                                   | MMA215170   | Numerical Optimization Techniques                   | 3 | 1 | 0 | 4         |
| <b>List of electives for 4<sup>th</sup> Semester</b> |             |                                                     |   |   |   |           |
| Sl. No.                                              | Course Code | Course Title                                        |   |   |   | CR        |
|                                                      |             |                                                     | L | T | P |           |
| 1                                                    | MMA 226050  | Artificial Intelligence and Hybrid Systems          | 3 | 1 | 0 | 4         |
| 2                                                    | MMA 226060  | Algebraic Number Theory                             | 3 | 1 | 0 | 4         |
| 3                                                    | MMA 226070  | Statistics III                                      | 3 | 1 | 0 | 4         |
| 4                                                    | MMA 226080  | Difference Equations and Discrete Dynamical Systems | 3 | 1 | 0 | 4         |
| 5                                                    | MMA 226090  | Coding Theory                                       | 3 | 1 | 0 | 4         |
| 6                                                    | MMA 226100  | Operator Theory                                     | 3 | 1 | 0 | 4         |
| 7                                                    | MMA 226110  | Operating Systems                                   | 3 | 1 | 0 | 4         |
| 8                                                    | MMA 226120  | Relational Database Management Systems              | 3 | 1 | 0 | 4         |
| 9                                                    | MMA 226130  | Classical Mechanics                                 | 3 | 0 | 1 | 4         |
| 10                                                   | MMA226140   | Tensor Algebra                                      | 3 | 0 | 1 | 4         |
|                                                      | MMA226150   | Differential Manifold                               |   |   |   |           |
|                                                      |             |                                                     |   |   |   |           |

### Semester-I

**Differential Equations**

**(3-1-0 4)**

Existence and uniqueness of solution to first order ordinary differential equation, Picard's iteration. Systems of first order differential equations, Trial solution method for a linear system with constant coefficients and Eigen value technique.

Simultaneous differential equations. Total (or Pfaffian) differential equations.

Orthogonal functions. Equations with regular singular points, power series solutions, Frobenius method. Bessel's Equation, Legendre equation, Hermite equation, Laguerre equation, Hypergeometric equation.

Sturm–Liouville problems and eigenfunction expansions: The Sturm–Liouville problem, Inner product spaces and orthonormal systems, basic properties of Sturm–Liouville eigenfunctions and eigenvalues, Nonhomogeneous equations, Nonhomogeneous boundary conditions, Green's functions.

Elements of Fourier analysis: The Fourier series of a function, convergence of Fourier series, Fourier Integral, Fourier transform and their convergence.

### **Texts/References**

1. M. Braun: Differential Equations and Their Applications, 3<sup>rd</sup> edition, Springer, 1983.
2. S. Padhy and J. Sinha Roy: A Course in Ordinary and Partial Differential Equations, 3<sup>rd</sup> edition, Kalyani, 2003.
3. W. E. Boyce and R. C. DiPrima: Elementary Differential Equation, 8<sup>th</sup> edition, Wiley, 2005.
4. C. H. Edwards and D. E. Penney: Elementary Differential Equations, 6<sup>th</sup> edition, Pearson, 2008.
5. J.R. Hanna and J.H. Rowland: Fourier series, Transforms, and Boundary Value Problems, Wiley, 1990.
6. J.W. Brown and R.V. Churchill: Fourier Series and Boundary Value Problems, 7<sup>th</sup> edition, McGraw Hill, 2008.
7. A. Vretblad: Fourier Analysis and its Applications, Springer, 2003.
8. E.A. Coddington and R. Carlson: Linear Ordinary Differential Equations, SIAM, 1997.

## **Mathematical Analysis**

**(3-1-0 4)**

### **Unit I Uniform Convergence**

Sequence of functions- point wise versus uniform convergence for a function defined on an interval of  $\mathbb{R}$ , Integration of a limit of a sequence of functions. The Weierstrass' approximation theorem. Periodic functions.

### **UNIT II – Functions of Several Variables**

Derivative of a function from an open subset of  $\mathbb{R}^n$  into  $\mathbb{R}^m$  as a linear transformation. Chain rule. Partial derivatives. Taylor's theorem. Inverse function theorem. Implicit function theorem, Jacobians.

### **Unit III Metric Spaces**

Review of compact metric spaces, Banach's contraction principle and its use in the proofs of Picard's theorem, inverse & implicit function theorems.

Baire category theorem and some of its applications in analysis of  $C(X)$  as a complete metric space when  $X$  is a compact metric space. Stone- Weierstrass theorem and Arzela-Ascoli theorem for  $C(X)$ .

### **Texts/References**

1. N.L. Carothers: Real Analysis, Cambridge University Press, 2000.
2. G. F. Simmons: Introduction to Topology and Modern Analysis, Tata McGraw-Hill, 2004.
3. P. K. Jain and V. P. Gupta: Lebesgue Measure and Integration, New Age International (P) Ltd., 2000.
4. G. De. Barra: Introduction to Measure Theory, New Age International (P) Ltd., 2000.
5. H. L. Royden and P. Fitzpatrick: Real Analysis, 4<sup>th</sup> edition, PHI, 2010.

### **Fundamentals of Computer and C Programming**

**(3-0-1 4)**

Introduction to computers, generations of computer, processors, memory hierarchy and I/O devices, System and application software, generation of languages, compiler, interpreter, assembler, Number systems, computer arithmetic.

Flow Charting, Sequential, Branching & Iterative.

Introduction to 'C' as Programming Language, An overview of a 'C' programme, 'C' character set, 'C' tokens, 'C' key words, Data Types (Primary, derived & user defined), Storage classes, symbolic constants, operators (arithmetic, logical & relational), Flow of control (if- else, switch-case; while, do-while & for-loops).

Functions (UDF, String Functions, Mathematical functions)

Recursion, pointers, array (2-D & 3-D), Strings, pre-processor directives, structures, linked list file handling.

C-lab: Execution of a simple programme, Conditional & Un-conditional Branching, Loops, Functions (Interactive & Recursive), Arrays (2-D & 3-D), Structures, Linked Lists, File I/O.

### **Texts/References**

1. B.W. Kernighan, D.M. Ritchie: The C Programming Language, Prentice Hall India, 1990.
2. Y.P. Kanetkar: Let us C, BPB Publications, 2002.
3. E. Balagurusamy: Programming in ANSI C, 4<sup>th</sup> edition, Tata McGraw Hill.

### **Numerical Analysis**

**(3-1-0- 4)**

**Unit I: Interpolation Theory:** Hermite Interpolation, the general Hermite interpolation, Spline interpolation problem.

**Approximation of functions:** The Minimax and Least squares approximation problem. Orthogonal polynomials, The Least squares approximation problem using orthogonal polynomials. Minimax and Near-minimax approximations.

**Unit II: Numerical Integration:** Gaussian Quadrature. Asymptotic error formulas and their applications. Automatic numerical integration. Multiple Integrals, Singular integrals.

**Unit III: Numerical Solution of Ordinary differential equations:** Numerical solutions of IVP – Difference equations, stability, error and convergence analysis. Single step methods - Taylor series method, Euler method, Picard's method of successive approximation, Runge-Kutta method. Multi step methods – Predictor-Corrector (PC) method, Euler PC method, Milne and Adams Moulton PC method. System of first order ODE, higher order IVPs. Numerical solutions of BVP – Linear BVP, finite difference methods, shooting methods, stability, error and convergence analysis, nonlinear BVP, higher order BVP.

**Numerical Solution of Partial Differential Equations.** – Initial/boundary value problems for parabolic and hyperbolic PDEs (one space and one time dimension). – Explicit finite-difference schemes. Implicit finite-difference schemes.

**Unit IV: Numerical solution of systems of linear equations:** Quick review of direct methods for solving linear systems, error analysis. The residual correction method. Iteration methods, Error prediction and Acceleration. **The Matrix Eigenvalue problem:** Review of Eigenvalue location, error, and stability results, Power method. Orthogonal transformations using Householder matrices. The eigenvalues of a symmetric Tridiagonal matrix. QR method. The calculation of Eigenvectors and Inverse iteration.

**Lab Components:** Exposure to MATLAB/Mathematica/SciLab and computational experiments based on the algorithms discussed in the course.

### Texts/References

1. K. Atkinson: An Introduction to Numerical Analysis, 2<sup>nd</sup> edition, Wiley, 1989.
2. R.L. Burden and J.D. Faires: Numerical Analysis, 7<sup>th</sup> edition, Brooks Cole, 2001.
3. S.D. Conte and C. de Boor: Elementary Numerical Analysis, 3<sup>rd</sup> edition, Tata McGraw Hill, 1980.
4. A. Iserles: A First Course in the Numerical Analysis of Differential Equations, Cambridge University Press, 1996.
5. P.J. Davis and P. Rabinowitz: Methods of Numerical Integration, 2<sup>nd</sup> edition, AP, 1984.
6. R. LeVeque: Finite Difference Methods for Ordinary and Partial Differential Equations Steady-State and Time-Dependent Problems, SIAM, 2007.
7. L. N. Trefethen and D. Bau III: Numerical Linear Algebra, SIAM, Philadelphia, 1997.
8. G. Sewell: The Numerical Solution of Ordinary and Partial Differential Equations, 2<sup>nd</sup> edition, Wiley, 2005.
9. E. Isaacson and H.B. Keller: Analysis of Numerical Methods, Dover, 1994.
10. P.J. Davis: Interpolation and Approximation, Dover, 1975.
11. J.M. Ortega: Numerical Analysis: A Second Course, SIAM, 1987.

A Quick review of matrices: Algebra of matrices, determinants, rank and nullity of matrices, system of linear equations, Symmetric, orthogonal and other special types of matrices, eigenvalues and eigen vectors of matrices, minimal and char. polynomial of a matrix, similar matrices, diagonalizable matrices.

Finite dimensional vector spaces over a field: Linear span, linear dependence and independence, basis and dimension. Linear transformation and rank-nullity theorem . Matrix representation of a Linear transformation. Matrix of Change of basis, algebra of linear operators, eigenvalues and eigenvectors, minimal and char. polynomial of a linear operator, Cayley-Hamilton theorem, transformation of linear operators to canonical forms: diagonal, triangular and Jordan forms.

Inner product spaces, Orthogonality, Gram-Schmidt orthogonalisation process, norms of vectors and matrices, linear functional, dual spaces, adjoint of an operator, normal, unitary, Hermitian and skew-Hermitian operators, Quadratic forms, reduction and classification of quadratic forms, Positive definite and negative definite matrices,

### **Texts/References**

1. P. D. Lax: Linear Algebra and Its Applications, 2<sup>nd</sup> edition, Wiley, 2007.
2. R. A. Horn and C.R. Johnson: Matrix Analysis, Cambridge University Press, 1990.
3. K. Hoffman and R. Kunze: Linear Algebra, 2<sup>nd</sup> edition, Prentice Hall, 1971.
2. P. R. Halmos: Finite-dimensional Vector Spaces, Springer, 1974.
3. C.D. Meyer: Matrix Analysis and Applied Linear Algebra, SIAM, 2000.
4. S.L. Campbell and C.D. Meyer: Generalized Inverses of Linear Transformations, SIAM, 2008.
5. A. J. Laub: Matrix Analysis for Scientists and Engineers, SIAM, 2004.
6. H. Anton and C. Rorres: Elementary Linear Algebra, Wiley India Edition 2009.
7. V. Krishnamurthy, V.P Mainra and J.L Arora: An Introduction to Linear Algebra, East-West Press, New Delhi 2011.

## **Semester-II**

### **Statistics- I**

**(3-1-0 4)**

**UNIT- I Introduction to Probability:** Concept of Random Experiment, Sample Space, Event, Definitions of Probability, Conditional Probability, Independent events and Mutually exclusive events. Addition and Multiplication Theorems, Bayes' Theorem.

**Random Variables and Probability Distributions:** Concept of a random variable, Discrete and Continuous Random Variables, Distribution Function, Probability Mass and Density Functions, Mathematical Expectation, Moment Generating Function, Characteristic Function, Probability Generating Function, Discrete and Continuous Probability Distributions such as Bernoulli, Binomial, Negative Binomial, Geometric, Hyper-Geometric, Poisson, Multinomial, Uniform, Exponential, Beta, Gamma and Normal.

## UNIT- II

**Joint Probability Distributions:** Introduction, Joint Distribution for Two Dimensional Random Variables, Marginal Distributions, Conditional Distributions, Covariance, Conditional Expectation, Independence of Random Variables, Distribution of Sum of Two Independent Random Variables.

**Sampling Distributions:** Sampling Distribution based on Normal Random Variables, t-Distribution, Chi-Square Distribution, F- Distribution, Order Statistics and their Distributions, Bivariate Normal Distribution, Multivariate Normal Distribution.

## UNIT- III

**Correlation and Regression Analysis:** Introduction, Types of Correlation, Karl Pearson's Coefficient of Correlation, Spearman's Rank Correlation, Multiple and Partial Correlation, Linear Regression Model, Regression Coefficient and its Properties, Computation of Regression Equation, Multiple Regression Analysis.

**Stochastic Process:** Introduction, Poisson Process, Birth and Death Process, Markov Chain, Transition Probabilities, Classification of States, Stationary Process.

### Texts/ References

1. S.M. Ross: Introduction to Probability and Statistics for Engineers and Scientists, Academic Press, 4<sup>th</sup> Edition, 2010.
2. W.W. Hines, D.C. Montgomery, D.M. Goldsman, and C.M. Borror: Probability and Statistics in Engineering, John Wiley and Sons, 4<sup>th</sup> Edition, 2007.
3. S.C. Gupta and V.K. Kapoor: Fundamentals of Mathematical Statistics, Sultan Chand and Sons, 2007.
4. A.M. Goon, M.K. Gupta, B. Dasgupta: Fundamental of Statistics, Vol. I, II, World Press, 2001.
5. V.K. Rohatgi and A.K. Ehsanes Saleh: An Introduction to Probability and Statistics, John Wiley and Sons, Inc. 2003.
6. G. Casella and R.L. Berger: Statistical Inference, Cengage Learning, 3<sup>rd</sup> Edition, 2008.
7. J. Medhi: Stochastic Processes, New Age Publication, 2<sup>nd</sup> Edition, 2002.

## Complex Analysis

(3-1-0 4)

Basic algebraic properties of complex numbers, Exponential form, Roots of complex numbers. Functions of a complex variable, mappings, Cauchy-Riemann equations, sufficient conditions for differentiability, Analytic functions, Harmonic functions. Elementary functions: The exponential, logarithm functions, branches and derivatives of logarithms. Complex exponents, trigonometric, hyperbolic functions and their inverses.

Integrals: Complex integrals, Upper bounds for moduli of contour integrals, Cauchy's theorem, Cauchy's integral formula, Liouville's theorem and fundamental theorem of algebra, maximum modulus principle. Series: Classification of singularities. Representations of holomorphic functions in terms of power series, Meromorphic functions, zeros and poles, Laurent expansions. Residues and Poles: poles and zeroes, Cauchy's residue theorem, Residue at infinity, Residue at poles. Evaluation of improper integrals and definite integrals

using contour integration. Argument principle and Rouché's theorem. Mapping by Elementary functions: Linear transformations, linear fractional transformations, other mappings by elementary functions. Conformal mapping: Preservation of angles, transformations of harmonic functions and boundary conditions. Applications of conformal mappings.

#### Texts/References

1. R. V. Churchill and J. W. Brown: Complex Variables and Applications, 8<sup>th</sup> edition, McGraw Hill, 2009.
2. L. Ahlfors: *Complex Analysis: an Introduction to the Theory of Analytic Functions of One Complex Variable*, 3<sup>rd</sup> edition, Tata McGraw Hill, 1979.
3. E.T. Copson: Theory of Functions of a Complex Variable, Oxford University Press, 1970.
4. J.B. Conway: Functions of One Complex Variable, 2<sup>nd</sup> edition, Narosa, 1973.
5. D. Sarason: Complex Function Theory, 2<sup>nd</sup> edition, Hindustan Publishing Company, 2008.
6. M.J. Ablowitz: Complex Variables Introduction and Applications, 2<sup>nd</sup> edition, Cambridge University Press, 2003.
7. S. Ponnusamy and H. Silverman: Complex Variables with Applications, Birkhäuser, 2006.

### Measure Theory and Integration

(3-1-0 4)

Lebesgue measure on  $R^n$ : Introduction, outer measure, measurable sets, Lebesgue measure, regularity properties, a nonmeasurable set, measurable functions, Egoroff's theorem, Lusin's theorem. Lebesgue integration: Simple functions, Lebesgue integral of a bounded function over a set of finite measure, bounded convergence theorem, integral of nonnegative functions, Fatou's Lemma, monotone convergence theorem, the general Lebesgue integral Lebesgue convergence theorem, change of variable formula. Differentiation and integration: Functions of bounded variations, differentiation of an integral, absolute continuity,  $L^p$ -spaces: The Minkowski's inequality and Holder's inequality, completeness of  $L^p$ , denseness results in  $L^p$ ; Fourier series: Definition of Fourier series, formulation of convergence problems,  $L^2$  theory of Fourier series, convergence of Fourier series.

#### Texts/References

1. P. K. Jain and V. P. Gupta: Lebesgue Measure and Integration, New Age International (P) Ltd., 2000.
2. G. De. Barra: Introduction to Measure Theory, New Age International (P) Ltd., 2000.
3. H. L. Royden, P. Fitzpatrick: *Real Analysis*, 4<sup>th</sup> edition, PHI, 2010.
4. W. Rudin, *Real and Complex Analysis*, 3<sup>rd</sup> edition, McGraw Hill Education, 1987.
5. G. B. Folland, *Real Analysis*, 2<sup>nd</sup> edition, Wiley, 1999.

### Topology

(3-1-0 4)

#### Unit I Topology.

**Topological Spaces:** Introduction, open set topology, Basis, Subbasis, closed sets and closure, Order Topology, Product Topology, Subspace Topology, Quotient Topology, Metric Topology, Continuous functions, Homeomorphisms, Open and Closed Maps.

**Unit-II Connectedness and Compactness:** Connected and Path Connected Spaces, Components and Path Components, Local Connectedness, Compact Spaces, Local compact spaces, Heine Borel Theorem, Tychonoff Theorem.

**Unit-III Countability and Separation Axioms:** Countability Axioms, Separation Axioms, Urysohn Lemma, Urysohn Metrization Theorem, Tietze extension Theorem.

### Texts/References

1. J. R. Munkres: Topology, Prentice Hall of India, 2001.
2. J. Dugundji: Topology, Universal Book Stall, New Delhi, 1990.
3. G. F. Simmons: Introduction to Topology and Modern Analysis, Tata McGraw-Hill edition, 2004.
4. M. D. Crossley: Essential Topology, Springer International Edition, 2008.

## Abstract Algebra

(3-1-0 4)

### Unit I

Groups: Quick review of basic ideas of Group Theory, Sylow's theorems and their applications, Finitely generated abelian groups.

### Unit II

Rings and ideals: Quick review in Commutative rings, Nilradical, Jacobson radical, Extension and Contraction, UFD, PID and ED, Rings of Fractions, Noetherian rings, Primary decomposition.

### Unit III

Modules: Introduction, Submodules and Quotient modules, Direct sum and Product, Finitely generated modules, Exact sequences, Tensor product of modules, Noetherian and Artinian modules, Modules of Fractions.

### Texts/References:

1. M. Atiyah: Introduction to Commutative Algebra, Westview Press, 1994.
2. D.S. Dummit and R.M. Foote: Abstract Algebra, 3<sup>rd</sup> edition, Wiley, 2003.
3. O. Zariski and P. Samuel: Commutative Algebra I. Vol. 1, Springer, 1975.
4. P. B. Bhattacharya, S. K. Jain, S. R. Nagpaul: Basic Abstract Algebra, 2<sup>nd</sup> edition, Cambridge, 1995.

## SEMESTER III

## Functional Analysis

(3-1-0 4)

Normed linear spaces: Finite dimensional normed spaces, Heine-Borel theorem, Riesz lemma, Continuity of linear maps, Hahn-Banach extension theorem, Banach spaces, Dual

spaces and transposes, Uniform-boundedness principle and its applications; Spectrum of a bounded operator.

Inner product spaces: Hilbert spaces, Orthonormal basis, Total Orthonormal Sets and Sequences Projection theorem and Riesz representation theorem. Representation of Functionals on Hilbert Spaces, Hilbert-Adjoint Operator, Self-Adjoint, Unitary and Normal Operators, Open Mapping Theorem, Closed Graph Theorem.

### **Texts/References**

1. E. Kreyszig: Introduction to Functional Analysis with Applications, Wiley, 1974.
2. J.B. Conway: A course in Functional Analysis, 2<sup>nd</sup> edition, Springer, Berlin, 1990.
3. A.N. Kolmogorov and S. Fomin: Elements of the theory of functions and functional analysis, Dover, 1999.
4. A. Taylor and D. Lay: Introduction to Functional Analysis, 2<sup>nd</sup> edition, Wiley, 1980.

## **Calculus of Variations and Integral Equations (3-1-0 4)**

**Calculus of Variations:** Introduction, problem of brachistochrone, problem of geodesics, isoperimetric problem, Variation and its properties, functions and functionals, Comparison between the notion of extrema of a function and a functional. Variational problems with the fixed boundaries, Euler's equation, special cases containing only some of the variables, Invariance of the Euler-Lagrange Equation, Functionals Containing Higher-Order Derivatives, Euler- Poisson equation, Functionals Containing Several Dependent Variables, System of Euler's equation, Functionals containing several independent variables, Ostrogradsky equation. Variational problems in parametric form, applications to differential equations. The Isoperimetric Problem and some of their generalizations. Applications to Eigenvalue Problems. Holonomic and Nonholonomic Constraints. Variational problems with moving boundaries, pencil of extremals, Transversality condition. Extremals with corners, refraction of extremals, examples, One-sided variations, conditions for one sided variations, Field of extremals, central field of extremals, The Hamiltonian Formulation, Jacobi's condition. The Weierstrass function, a weak extremum, a strong extremum. The Legendre condition, Conjugate Points, Variational methods for boundary value problems in ordinary and partial differential equations.

**Integral Equations:** Introduction and basic examples, Classification, Conversion of Volterra Equation to ODE, Conversion of IVP and BVP to Integral Equation, Successive approximation, Successive substitution methods for Fredholm Integral Equations, series solution, successive approximation, successive substitution method for Volterra Integral Equations, Volterra Integral Equation of first kind, Integral Equations with separable Kernel, Fredholm's first, second and third theorem, Integral Equations with symmetric kernel, Eigen functions expansion, Hilbert-Schmidt theorem, Fredholm and Volterra Integro-Differential equation, Singular Integral Equation.

### **Texts/References**

1. B. Brunt: The Calculus of Variations, Springer-Verlag, New York, 2004.

2. F. Y. M. Wan: Introduction to the Calculus of Variations and its Applications, 2<sup>nd</sup> edition, Chapman & Hall, 1995.
3. M. Gelfand and S. V. Fomin: Calculus of Variations, Prentice Hall, 1963.
4. R. Weinstock: Calculus of Variations with Applications to Physics and Engineering, Dover, 1974.
5. R. Courant and D. Hilbert: Methods of Mathematical Physics, Vol I. John Wiley & Sons, 1989.
6. L.E. Elsgolc: Calculus of Variations, Pergamon Press Ltd., 1962.
2. D. Porter and D. S. G. Stirling: Integral Equations - A Practical Treatment from Spectral Theory and Applications, Cambridge University Press, 1990.
3. C. Corduneanu: Integral Equations and Applications, Cambridge University Press, 1991.
4. S. G. Mikhlin: Integral Equations, Hindustan Publishing Co., 1960.
5. E. G. Tricomi: Integral Equations, Interscience, 1957.
6. 11. F. B. Hildebrand: Methods of Applied Mathematics, 2<sup>nd</sup> edition, Prentice Hall, 1965.

### Partial Differential Equations

(3-1-0 4)

Introduction to partial differential equations. Solution of linear and nonlinear partial differential equations of order one. Introduction to Cauchy's problem. Homogeneous and non-homogeneous linear partial differential equations.

Classification of partial differential equations, reduction to canonical or normal form. Monge's method, second order Cauchy Problem.

**Wave equation:** d'Alembert solution of the Cauchy problem, the characteristic triangle, Fourier series solution. A Wave equation in two space dimensions, The Kirchhoff-Poisson solution, Hadamard's method of Descent.

**Heat Equation:** The Cauchy problem and initial conditions, Solution of homogenous and non-homogenous problem, heat kernel. the heat equation in two space variables.

**Laplace's equation: Dirichlet and Neumann Problems** Harmonics functions, Dirichlet problems, Poisson's integral representation, The Neumann problem, Green's function, conformal techniques, existence theorems, solutions by Eigen function expansions.

**Elliptic equations:** Existence of weak solutions, The maximum principle, Green's identities.

### Texts/References

1. P.V. O'Neil: Beginning Partial Differential Equations, 2<sup>nd</sup> edition, Wiley, 2008.
2. Y. Pinchover and J. Rubinstein: An Introduction to Partial Differential Equations, Cambridge University Press, 2005.
3. R. Haberman: Applied Partial Differential Equations with Fourier Series and Boundary Value Problems, 4<sup>th</sup> edition, Pearson, 2004.
4. M. D. Raisinghania: Ordinary and Partial Differential Equations, 12<sup>th</sup> edition, S. Chand, 2010.
5. R. Agarwal and D. O'Regan: Ordinary and Partial Differential Equations. With Special Functions, Fourier Series, Boundary Value Problems, Springer 2009.
2. L.C. Evans: Partial Differential Equations, AMS, 1998.

3. E. A. Coddington and N. Levinson: Theory of Ordinary Differential Equations, Tata McGraw Hill, 1987.

### Semester-III-Electives

#### Theory of Computations

(3-1-0 4)

**Unit 1:** Chomsky Hierarchy: regular grammars, unrestricted grammars, context sensitive languages, relations between classes of languages. Finite Automata and Regular Expressions: Deterministic and non-deterministic finite automata, regular expressions, Two way finite automata, finite automata with output: Mealy and Moore machines; Properties of Regular Sets: Pumping lemma, closure properties, decision algorithm, Myhill-Nerode theorem and minimization of finite automata.

**Unit 2:** Context-Free Grammars (CFG): CFGs, derivation trees, simplification, Chomsky normal forms, Greibach normal forms; Pushdown Automata (PDA): Definitions, relationship between PDA and context free languages, Properties of Context-Free Languages, Pumping lemma, closure properties, decision algorithm; Turing Machines: The turing machine model, computable languages and functions, techniques for turing machine construction, modification of turing machines, Church's hypothesis, Turing machines as enumerators;

**Unit 3:** Decidability: Decidable Languages, The Halting problem, Reducibility. Undecidability: properties of recursive and recursively enumerable languages, universal Turing machines, rice's theorem, post correspondence problem, Greibach's theorem, Introduction to recursive function theory; Complexity Theory: Measuring complexity, The P, NP, NP-Hard and NP completeness.

#### Texts/References

1. K.L.P. Mishra and N. Chandrasekharan: Theory of Computer Science: Automata Language and Computation, Prentice Hall of India, 3<sup>rd</sup> edition, 2007.
2. P. Linz: Introduction to Formal Language and Computation, Narosa, 2<sup>nd</sup> edition, 2006.
3. M. Sipser: Introduction to the Theory of Computation, Thomson Learning, 2001.
4. J. Martin: Introduction to Languages and the Theory of Computation, 3<sup>rd</sup> edition, McGraw Hill, 2002.
5. J. E. Hopcroft, R. Motwani and J.D. Ullman: Introduction to Automata Theory, Languages and Computation, 2<sup>nd</sup> Edition, Pearson Education, 2001.

#### Field Theory

(3-1-0 4)

Unit I: Fields, finite fields, Polynomial rings and irreducibility criteria. Field extensions, Algebraic field extensions.

Unit II: Normal and Separable Extensions, Galois extensions, Fundamental Theorem of Galois Theory.

Unit III: Constructibility by ruler and compass, Solvability by radicals, Insolvability of the general quintic by radicals.

### Text/References

1. P. B. Bhattacharya, S. K. Jain, S. R. Nagpaul: Basic Abstract Algebra, 2<sup>nd</sup> edition, Cambridge, 1995.
2. M. Artin: Algebra, Prentice Hall India, 2009.
3. S. Lang: Algebra, 3<sup>rd</sup> edition, Springer, 2002.
4. J. Rotman: Galois Theory, 2<sup>nd</sup> edition, Springer, 2006.
5. P. Morandi: Field and Galois Theory, Springer, 2010.
6. I. S. Luthar and I. B. S. Passi: Algebra 4 - Field Theory, Narosa, 2004.

## Statistics- II

(3-1-0 4)

### UNIT- I

**Inequalities and Limit Theorems:** Introduction, Markov's Inequality, Chebyshev's Inequality, One-sided Chebyshev Inequality, Jensen's Inequality, Random Sample, Modes of Convergence of a sequence of random variables: Convergence in Distribution, Convergence in Probability, Convergence Almost Sure; Weak Law of Large Numbers (WLLN), Strong Law of Large Numbers (SLLN) and Central Limit Theorems (CLT).

### UNIT- II

**Theory of Estimation:** Introduction, Point Estimation and Interval Estimation, Methods of Estimation: Method of Maximum Likelihood, Method of Moments; Properties of Estimators: Unbiasedness, Consistency, Efficiency, Sufficiency; Minimum Variance Unbiased Estimator (MVUE), Cramer-Rao Inequality, Minimum Variance Bound (MVB) Estimator, Bayes Estimators.

**Confidence Interval (CI) Estimation:** Introduction, CI on Mean and Variance of a Normal Distribution, CI on a Proportion, CI on the difference between Means for Paired Observations, CI on the ratio of Variances of Two Normal Distributions, CI on the difference between Two Proportions.

### UNIT- III

**Tests of Hypotheses:** Introduction, Statistical Hypotheses, Type-I and Type-II Errors, One-Sided and Two-Sided Hypotheses, Tests of Hypotheses on the Mean of a Normal Distribution; Variance Known as well as Unknown Cases, Tests of Hypotheses on the Variance of a Normal Distribution, Tests of Hypotheses on a Proportion, Tests of Hypotheses on the Means of Two Normal Distributions; Variances Known as well as Unknown Cases, The Paired t-Test, Tests for Equality of two Variances, Tests of Hypotheses on two Proportions, Testing for Goodness of Fit, Contingency Table Tests, Neyman-Pearson Theory of Testing of Hypotheses, Uniformly Most Powerful Tests, Likelihood Ratio Tests, Unbiased Tests.

### Texts/ References

1. S.M. Ross: Introduction to Probability and Statistics for Engineers and Scientists, Academic Press, 4<sup>th</sup> Edition, 2010.
2. W.W. Hines, D.C. Montgomery, D.M. Goldsman, and C.M. Borror: Probability and Statistics in Engineering, John Wiley and Sons, 4<sup>th</sup> Edition, 2007.

3. S.C. Gupta and V.K. Kapoor: Fundamentals of Mathematical Statistics, Sultan Chand and Sons, 2007.
4. A.M. Goon, M.K. Gupta, B. Dasgupta: Fundamental of Statistics, Vol. I, II, World Press, 2001.
5. V.K. Rohatgi and A.K. Ehsanes Saleh: An Introduction to Probability and Statistics, John Wiley and Sons, Inc. 2003.
6. G. Casella and R.L. Berger: Statistical Inference, Cengage Learning, 3<sup>rd</sup> Edition, 2008.
2. S. Ross: A First Course in Probability, 8<sup>th</sup> Edition, Pearson Education, 2010.

## Discrete Mathematics

(3-1-0 4)

### Unit I

Pigeon Hole Principle, Inclusion Exclusion Principle, Techniques of Counting, Recurrence relations.

### Unit II

Mathematical Logic, Truth Table, Introduction to Lattice theory, Boolean algebra with application to switching circuits.

### Unit III

Introduction to Graph Theory, Basic terms of graph theory, handshaking theorem, Eulerian Graph, Hamiltonian Graph, Planar Graph, Colouring of Graphs, Colouring problem, Five colour Theorem.

### Texts/References

1. K. D. Joshi: *Foundations of Discrete Mathematics*, New Age International Pb., 1996.
2. R. A. Brualdi, *Introductory Combinatorics*, Fifth Edition, Pearson Education, 2009.
3. R. J. Wilson, *Introduction to Graph Theory*, Fifth edition, Printice Hall, 2010.
4. A. Bondy, U. S. R. Murty, *Graph Theory*, Springer Verlag, 2008.
5. J. P. Tremblay and R. Manohar, *Discrete Mathematical Structures with Application to Computer Science*, Tata McGraw-Hill, 2008.

## Fluid Dynamics

(3-1-0 4)

Lagrangian and Eulerian description, stream lines, path lines, streak lines, vortex lines, vorticity vector, equation of continuity, circulation, rotational and irrotational flows, boundary surface. General equations of motion, Bernoulli's theorem ( Compressible , incompressible flows) Kelvin's theorem (constancy of circulation). Stream function, complex potential, sources, sinks and doublets, Circle theorem, Method of images. Theorem of Blasius. Viscous flows- stress analysis in fluid motion, relations between stress and rate of strain. Stoke's stream function, Spherical Harmonics and motion of a Sphere. Helmholtz's vorticity equation (permanence of vorticity) Vortex filaments, vortex pair. Navier-Stoke's equations. Dissipation of energy. Diffusion of vorticity, Steady flow between two infinite parallel plates, through a circular pipe (Hagen Poiseuille flow).

### Text/References

1. R.W. Fox et.al. Introduction to Fluid Mechanics, 7<sup>th</sup> edition, Wiley, 2009.
2. B.R. Munson et.al. Fundamentals of Fluid Mechanics, 6<sup>th</sup> edition, Wiley, 2009.
3. A.K. Mohanty: Fluid Mechanics, 2<sup>nd</sup> edition, PHI, 2009.
4. M.D. Raisinghania: Fluid Dynamics, 9<sup>th</sup> edition, S. Chand, 2010.
5. F. Durst, Fluid Mechanics: An introduction to the Theory of Fluid Flows, Springer, 2008.

### **Theory and Applications of Fuzzy Sets**

**(3-1-0 4)**

Basic concepts of fuzzy sets, fuzzy logic, operations on fuzzy sets, fuzzy relations, equivalence and similarity relations, ordering, morphisms, fuzzy relation equations, fuzzy measures, probability measures, possibility and necessity measures, measures of uncertainty, dissonance, confusion and nonspecificity. Principles of uncertainty and information. Applications of fuzzy sets in management, decision making, computer science and systems science.

#### Texts/References:

1. T. J. Ross: Fuzzy Logic with Engineering Applications, 3<sup>rd</sup> edition, Wiley, 2010.
2. G. J. Klir and B. Yuan: Fuzzy Sets and Fuzzy Logic Theory and Applications, Prentice Hall, 1995.
3. G. Chen and T. Pham: Introduction to Fuzzy Sets, Fuzzy Logic, and Fuzzy Control Systems, CRC, 2000.
4. H. J. Zimmermann: Fuzzy Set Theory - and Its Applications, 2<sup>nd</sup> edition, Springer, 1991.

### **Data Structures and Algorithm Analysis (2-1-1 4)**

#### **Unit I: Data and Algorithms**

Introduction to Data, Information and structures of Data, Algorithms (Quick Review with algorithm design techniques). Introducing uses of data structures in algorithms ( fundamental examples).

Types of Data Structure: Linear and Non-Linear.

Array, Linked List. Stack, Queue (s), Graph (s) (Quick review to type and its properties) and Trees (Binary and others), Priority Queue, Heaps (Binary). Stack and Queue using Array and Linked List.

#### **Unit II: Asymptotic analysis**

Introduction to Algorithms' analysis, cost of algorithms in terms of steps (time) and space (memory).

Asymptotic Notations and analysing algorithms. growth of functions (Graph representation). Recurrence and asymptotic notations, solving recurrences (Master theorem), Problems practices.

#### **Unit III: Algorithms and analysis**

**Searching:** Linear, Binary, B-Tree, DFS, BFS, Binary Search Tree, AVL Search Tree, Hashing.

**Sorting:** Finding max, min and sorting, Insertion Sort, Bubble Sort, Selection Sort, Heap sort, Quick sort, Merge sort, String sort.

Strassen's matrix multiplication, Sum of subsets, Minimum spanning trees, Shortest Path algorithm.

## **Computer Experiments using C Programming Language**

### Texts/References:

1. Expert Data Structures with C by R.B. Patel; Khanna Publishers, New Delhi.
2. Algorithms + Data Structures = Programs by Niklaus Wirth; Prentice Hall, 1976.
3. Horowitz and Sahani: Fundamentals of Computer Algorithms.
2. T.H. Cormen, C.E. Leiserson, R.L. Rivest and C. Stein: Introduction to Algorithms, 20<sup>th</sup> edition,
3. Prentice Hall India, 2010.
4. Shaurm's Outline Series by Lipschutz; McGraw Hill Education P Ltd , New Delhi.

## **Cryptography**

**(3-1-0 4)**

Introduction to basic terminologies associated with Cryptography, Definition and classification of Cryptosystem, Classical crypto systems, Description of rail fence cipher, Simple Columnar cipher, Caesar cipher, Linear cipher, Affine linear cipher, Distinction between Substitution cipher and Permutation cipher. Classical cipher as particular case of Affine linear cipher, Insecurity of Affine linear cipher, Block cipher and different modes of implementation of Block cipher, Stream cipher, Feistel cipher, DES (Data Encryption Standard) and AES (Advanced Encryption Standard).

Public Key cryptosystems, Need for Public Key cryptosystems, Description of RSA, Rabin cryptosystem, Diffie-Hellman key exchange, ElGamal cryptosystem, Cryptanalysis of Public Key cryptosystem, Digital signatures, Introduction to Elliptic curve cryptography, Perfect security and Shannon's Theorem. Mathematical problems related to cryptography, Division Algorithm and extended Division Algorithm, Calculation of Units in  $\mathbb{Z}/n\mathbb{Z}$ , Fast Exponentiation, Factoring problem, Different factorisation Algorithms, Discrete Log Problem, Discussion of different algorithms for finding discrete log.

**Lab Component:** Cryptography Lab in C (at least 10 Sessions), Use of Sage software.

### Texts/References

1. J. A. Buchmann: Introduction to Cryptography, Springer, 2004.
2. N. Koblitz: A Course in Number Theory and Cryptography, Springer, 1994.
3. M. Welschenbach: Cryptography in C and C++, 2<sup>nd</sup> edition, Apress, 2002.

## **JAVA Programming**

**(3-0-1-4)**

History of java, Features of java, JVM Architecture, Data Types, Operators, Arrays, Command Line Arguments, OOPS in java, Abstract Classes, Interfaces, Packages, Access modifiers, Access Specifiers, Exception Handling, Applet, Multithreading, Streams(File

I/O), Introduction to AWT, Introduction to Collection Framework (java.util.\*), String Handling.

Lab: JAVA lab.

### **Text/References**

1. H. Schildt: The complete Reference, 8th Edition, Tata McGraw Hill, 2011.
2. K. Sierra, B. Bates; SCJP Sun certified Programmer for java 6 study Guide, Tata McGraw Hill, 2008.
3. E. Balagurusamy: Programming with java, 4th Edition Tata McGraw Hill 2009.

## **Graph Theory**

**(3-1-0 4)**

Graphs and Sub graphs:- Graphs and simple graphs, Graph isomorphism, The incidence and adjacency matrices, sub graphs, connected and bipartite graphs, walk, trail, path and cycles.

Application:- The Shortest path problem, Dijkstra algorithm, Warshall Algorithm.

Trees:- Trees, Cut Edge and Bond, Cut vertex, spanning trees and Cayley's formula. The Connector Problem: Prim's Algorithm, Kruskal's Algorithm.

Euler tour and Hamilton's Cycles, characterization of Eulerian graphs, a necessary and some sufficient characterizations of Hamiltonian graph. Closure and degree majorization and related results, Chinese Postman Problem.

Matchings: Theorem of Berge, Matchings and coverings in Bipartite graphs, Application: Hall's marriage theorem, Some Assignment Problems.

Connectivity: m-connectivity and blocks, Construction of Reliable Communication Networks.

Vertex Coloring: Planar graph, Euler's formula, Chromatic Number, Brook's Theorem, 5-color theorem.

**Lab Component:** Implementation in C: Dijkstra Algorithm, Warshall Algorithm, BFS, DFS, Prim's Algorithm, Kruskal Algorithm, Connectivity Algorithm, Flurey Algorithm.

### **Text/References**

1. J.A. Bondy and U.S.R Murty: Graph Theory, Springer, 2008.
2. F. Harary: *Graph Theory*, Westview Press, 1994.
3. R.J. Wilson: Introduction to Graph Theory, 4<sup>th</sup> edition, Pearson, 2002.
4. J. Clark and D. A. Holton: A First Look at Graph Theory, World Scientific, 1991.
5. D.B. West: Introduction to Graph Theory, 2<sup>nd</sup> edition, PHI Learning, 2009.
6. N. Deo: Graph Theory with Applications to Engineering and Computer Science, Prentice-Hall of India, 2004.

## **Mathematical Modelling**

**(3-1-0 4)**

Introduction to modelling, Mathematical modelling, Types of models, Characteristics of Mathematical models, Models on algebraic systems.

Modelling with Difference Equations: overview of basic concepts concerning matrices, eigenvalues and eigenvectors; fixed points, stability and iterative processes; applications to population growth.

Mathematical Models based on Ordinary differential equations, Models based on system of ordinary first order differential equations. Motion of satellites, Electrical Circuits, A curve and Pursuit, Birth & Deaths model, Logistic model for growth, Models in Economics and Finance.

Empirical Modelling with Data Fitting: error function, least squares method; fitting data with polynomials and splines. Types of Simulation, Simple Case Studies, Simulation methodology, Simulation Software, Criteria for valid and Creditable Simulation Models.

Mathematical models through Partial Differential equations: Equation of Continuity in fluid flow, Heat flow and Traffic flow. Diffusion models in air pollution, Water pollution, simple models based on heat transfer, mass transfer and wave propagation.

### **Texts/References**

1. J.N. Kapoor: *Mathematical Modelling*, Wiley Eastern Ltd, 1982.
2. R. Haberman: *Mathematical Models: Mechanical Vibrations, Population Dynamics, and Traffic Flow*, SIAM, 1998.
3. M. Braun: *Differential Equations and their Application: An Introduction to Applied Mathematics*, 3<sup>rd</sup> edition, Springer, 1991.
4. A.M. Law: *Simulation Modelling and Analysis*, 4<sup>th</sup> edition, McGraw Hill, 2006.
5. R. M. Davies and R. M. O'Keefe: *Simulation Modelling with Pascal*, Prentice Hall 1989.
6. F. R. Giordano, W.P. Fox and S. B. Horton: *A First Course in Mathematical Modelling*, 5<sup>th</sup> edition, Cengage Learning, 2013.

### **Integral Transforms**

**(3-1-0 4)**

**Unit-I: Laplace Transform:** Definition, Transform of some elementary functions, rules of manipulation of Laplace Transform, Transform of Derivatives, relation involving Integrals, the error function, Transform of Bessel functions, Periodic functions, convolution of two functions, Inverse Laplace Transform of simple function, Tauberian Theorems, Solution of Differential Equations- Initial value problems for linear equations with constant coefficients, two-point boundary value problem for a linear equation with constant coefficients, linear differential equation with variable coefficients, simultaneous differential equations with constant coefficients, Solution of diffusion and wave equation in one dimension and Laplace equation in two dimensions.

**Unit-II: Fourier Series and Fourier Transforms:** Orthogonal set of functions, Fourier series, Fourier sine and cosine series, Half range expansions, Fourier integral Theorem, Fourier Transform, Fourier Cosine Transform, Fourier Sine Transform, Transforms of Derivatives, Fourier transforms of simple Functions, Fourier transforms of Rational Functions, Convolution Integral, Parseval's Theorem for Cosine and Sine Transforms, Inversion Theorem, , Solution of Partial Differential Equations by means of Fourier Transforms. First order and second order Laplace and Diffusion equations.

### **Unit-III: Mellin transform and its properties. Z-Transform with its properties.**

#### **Books Recommended:**

1. Ian N. Sneddon , The use of Integral Transforms ,McGraw Hill; Second Printing edition ,1972.
2. Ian N. Sneddon, Fourier Transforms, Dover Publications, 2010.
3. LoknathDebnath, Integral Transforms and their applications, Chapman and Hall/CRC; 2 edition, 2006.
4. R. K. Jain, S. R. K. Iyengar : *Advanced Engineering Mathematics* , Fifth Edition.
5. Murray Spiegel: Schaum's Outlines of Laplace Transform.
6. Murray Spiegel: Schaum's Outlines of Fourier Analysis with Applications to Boundary Value Problems.

### **Numerical Optimization Techniques**

**(3-1-0 4)**

Introduction: Optimization, Types of Problems and Algorithms. Convex Sets and Convex Functions, Unconstrained Optimization: Basic properties of solutions and algorithms, Global convergence, Basic Descent Methods: Line Search Methods, Steepest Descent and Newton Methods, Modified Newton methods, Globally convergent Newton Method. Nonlinear Least Squares Problem and Algorithms, Conjugate Direction Methods, Trust-Region Methods. Lab Component: Exposure to Matlab/Mathematica and computational experiments based on the algorithms discussed in the course.

#### **Texts/References**

1. E.K.P. Chong and S.H. Zak: *An Introduction to Optimization*, 2<sup>nd</sup> edition, Wiley, 2001.
2. R. Fletcher: *Practical Methods of Optimization*, 2<sup>nd</sup> edition, Wiley, 2000.
3. S. S. Rao: *Engineering Optimization: Theory and Practice*, 4<sup>th</sup> edition, Wiley, 2009.
4. D. Luenberger and Y. Ye: *Linear and Nonlinear Programming*, 3<sup>rd</sup> edition, Springer, 2008.
5. M.S. Bazaraa et al.: *Nonlinear Programming - Theory and Algorithms*, 3<sup>rd</sup> edition, Wiley, 2006.

#### **Course Learning Outcomes:**

Upon successful completion, students will have the knowledge and skills to: Use sophisticated scientific computing and visualization environments to solve application problems involving matrix computation algorithms, Analyze numerical algorithms, and understand the relationships between the computational effort and the accuracy of these algorithms, Interpret the results produced by computer implementations of numerical algorithms, Explain the effects of errors in computation and how such errors affect solutions, Demonstrate the necessary analytical background for further studies leading to research in applied mathematics or related disciplines.

### **Semester-IV**

**UNIT- I**

**Linear Programming:** Introduction, Linear Programming Problem (LPP) and its formulation, Graphical method for solving LPP, Basic Feasible Solution, Simplex Method, Big-M and Two-phase methods, Degeneracy, Alternative Optimal Solution, Unbounded Solution, Infeasible Solution, Dual Problem and Duality Theorems, Dual Simplex Method and its application in post-optimality analysis.

**UNIT- II**

**Transportation and Assignment Problems:** Introduction, Transportation algorithm, Mathematical formulation, Balanced and Unbalanced Transportation Problems, Vogel's approximation method for solving Transportation Problems, Hungarian method for solving Assignment Problems.

**UNIT- III**

**Queuing and Inventory Theory:** Introduction, Queuing System, Elements of a Queuing System, Operating Characteristics, Probability distributions in Queuing Systems, Elementary Queuing and Inventory Models, Steady-state solutions of Markovian Queuing Models: M/M/1, M/M/1 with limited waiting space, M/M/C, M/M/C with limited waiting space, M/G/1.

**Texts/ References**

1. E.K.P. Chong and S.H. Zak: An Introduction to Optimization, 2<sup>nd</sup> edition, Wiley, 2001.
2. D.G. Luenberger, Y. Ye: Linear and Nonlinear Programming, 3<sup>rd</sup> edition, Springer, 2008.
3. A.Ravindran, K.M. Ragsdell, G.V. Reklaitis: Engineering Optimization, 2<sup>nd</sup> edition, Wiley, 2006.
4. H.A. Taha: Operations Research: An Introduction, 8<sup>th</sup> edition, Prentice Hall, 2007.
5. K. Swarup, P. K. Gupta and M. Mohan: Operations Research, Sultan Chand and Sons, 2004.

**Number Theory****(3-1-0 4)**

Unit I: Fundamental theorem of arithmetic, divisibility in  $\mathbb{Z}$ , congruences, Chinese Remainder Theorem, Euler's  $\phi$ - function, primitive roots, Fermat's Little, Euler and Wilsons Theorem.

Unit II: Linear Congruence, Algebraic congruences of degree  $\geq 2$ . Theorems on Prime Power, Modulus, Lagrange Theorem, Quadratic Congruences, Quadratic reciprocity law, two square theorem, Primality Testing and Factoring.

Unit III: Simple continued fractions, Pell's Equation, Diophantine Approximation. Arithmetical functions. Sum and number of Divisors, Dirichlet Product, Mobius inversion formula, Totally multiplicative functions.

**Texts/References**

1. G.H. Hardy and E.M. Wright: An Introduction to The Theory of Numbers, 6<sup>th</sup> edition, Oxford University Press, 2008.
2. D.M. Burton: Elementary Number Theory, 6<sup>th</sup> edition, McGraw-Hill, 2005.
3. I. Niven, H.S. Zuckerman and H.L. Montgomery: An Introduction to The Theory of Numbers, 5<sup>th</sup> edition, Wiley, 1991.
5. T. M. Apostol: Introduction to Analytic Number Theory, Springer- Verlag, 1976.

## Electives of Semester IV

### Artificial Intelligence and Hybrid Systems

(3-1-0 4 )

#### Unit I : Artificial Intelligence

Overview of AI, Knowledge representation, Mappings, Approaches and issues, Predicate logic, Propositional logic, Procedural and declarative knowledge.

**Fuzzy Logic:** Fuzzy Sets, Fuzzy Relations, Fuzzy operations (on fuzzy sets), Fuzzy numbers and arithmetics, Fuzzy Logic and Possibility Theory.

**Problem space and searching techniques** (Algorithms and Problem Practices): Heuristic search technique (s), State Space Search, Graph Search, Search Based on Recursion, Pattern-directed Search.

#### Unit II : Machine Learning

Introduction, training data, function approximation, Learning Input-Output Functions, Performance Evaluation.

**Learning** (Algorithms and Problem Practices): Decision Tree based, Error correction learning, Supervised, Unsupervised, Hebbian learning, Clustering, K-Means Clustering, Credit assignment problem, Bayes Theorem and Classification.

#### Unit III: Intelligent Systems

Introduction, Cognitive Science, Expert Systems, Stages in the Development, Probability-based Expert Systems, Example of Chess game (Practice with 8-Queens problem)

#### Unit IV : Artificial Neural Networks

Neural network, human brain, model of an artificial neuron, mathematical preliminaries, taxonomy of NN, classical artificial intelligence and neural network.

**Artificial Neural Network:** Feed-forward network, Feed-backward network, Recurrent Network, Single Layer and Multi-layer Networks, Perceptron (example of Rosenblatt perceptron)

**Single layer Perceptrons** (Algorithms and Problem Practices): Adaptive Filtering Problem, unconstrained optimization techniques, linear least square algorithm, perceptron convergence theorem.

**Multilayer Perceptrons:** Back propagation algorithm, XOR problem, output representation and decision rule, back propagation and differentiation.

**Geometry of Binary Threshold Neurons:** Pattern recognition and data classification, convex sets, convex hulls and linear separability, space of Boolean functions, binary neurons are pattern dichotomizers, non-linear separable problems, capacity of a simple threshold logic neurons, Re-visiting the XOR problem.

Unit V : Hybrid systems, Decision Making Systems, Neuro- fuzzy systems

**Texts/References:**

1. Artificial Intelligence: Elaine Rich, Kevin Knight, Mc-Graw Hill.
2. Introduction to AI & Expert Systems: Dan W. Patterson, PHI.
3. G. J. Klir & B. Yuan, Fuzzy sets & Fuzzy logic by PHI.
4. Introduction To Machine Learning, Nils J. Nilsson.
5. C. M. Bishop: Pattern Recognition and Machine Learning, Springer, 2006.
6. S. Kumar: Neural Networks – A Classroom Approach, Tata McGraw-Hill, 2003.
7. Da Ruan: Intelligent hybrid systems: Fuzzy logic, neural networks, and genetic algorithms, Kluwer academic Publishers 1997.

**Algebraic Number Theory**

(3-1-0 4)

Unit I

Algebraic Numbers and Algebraic Integers, Algebraic Number Fields, Integral Basis and Discriminant, Ring of Integers in an Algebraic Number Field (with explicit calculations for Quadratic & Cyclotomic fields).

Unit II

Divisibility in Algebraic Number Fields, Euclidean Fields, Group of Units in an Algebraic Number Field, Divisibility in Quadratic Fields.

Unit III

Ideals, Divisors and Factors, Fundamental Theorem of Ideal Theory, Fractional Ideals, Inverse of an Ideal, Congruences, Norm of an Ideal, The problem of ramification, Class numbers, The Fermat conjecture.

**Texts/References**

1. Harry Pollard, Harold G. Diamond: The Theory of Algebraic Numbers, 3<sup>rd</sup> edition, Dover, 2010.
2. S. Alaca, K. S. Williams: Introductory Algebraic Number Theory, CUP, 2003.
3. E. Weiss: Algebraic Number Theory, Dover, 1998.
4. Stewart, D. Tall: Algebraic Number Theory and Fermat's Last Theorem, 3<sup>rd</sup> edition, A K Peters/CRC Press, 2001.
5. G. J. Janusz: Algebraic Number Fields, 2<sup>nd</sup> edition, 1996.

**Statistics III**

(3-1-0 4)

**Sampling Theory:** Introduction, Concept of Population and Sample, Primary and Secondary data, Methods of Collecting Primary data, Sampling frame, Sampling design, Determination of sample size, Census and Sample Surveys, Sampling and Non-sampling errors, Simple Random Sampling, Stratified Sampling, Systematic Sampling, Probability Proportional to Size (PPS) Sampling, Ratio and Regression Methods of Estimation.

**Design and Analysis of Experiments:** Introduction, Analysis of Variance (ANOVA) and Analysis of Covariance (ANCOVA), Fixed, Random and Mixed effects Models, ANOVA for one-way and two-way Classified Data, Basic principles of Design of Experiments, Completely Randomized Design (CRD), Randomized Block Design (RBD) and Latin Square Design (LSD), Factorial Experiments, Confounding in symmetrical factorial experiments ( $2^n$  series), Connectedness and Orthogonality of Block Designs, Balanced Incomplete Block Design (BIBD).

### Texts/ References

1. W. G. Cochran: Sampling Techniques, John Wiley and Sons, 3<sup>rd</sup> Edition, 1977.
2. P. V. Sukhatme, B. V. Sukhatme, S Sukhatme & C. Ashok : Sampling Theory of Surveys with Applications, Iowa State University Press and Indian Society of Agricultural Statistics, New Delhi, 1984.
3. W. G. Cochran & D. R. Cox : Experimental Designs, John Wiley, 1957.
4. D. C. Montgomery: Design and Analysis of Experiments, John Wiley and Sons, 8<sup>th</sup> Edition, 2013.
5. S.C. Gupta and V.K. Kapoor: Fundamentals of Applied Statistics, Sultan Chand and Sons, 1994.
6. M.N. Das and N.C. Giri: Design and Analysis of Experiments, New Age Publication, 2<sup>nd</sup> Edition, 1986.

## Difference Equations and Discrete Dynamical Systems

(3-1-0 4)

**Difference Equations:** Introduction to Difference Equations, First order DEs, linear equations with constant coefficients, variable coefficients, stability in both hyperbolic and nonhyperbolic cases, bifurcations, symbolic dynamics and chaos, linear theory for two dimensional systems of difference equations, equilibria, stability, periodic solutions, period-doubling bifurcation, Lyapunov numbers, box dimension, stable and unstable manifolds, area preserving maps, systems with order higher than 2, numerical issues in difference equations.

**Discrete Dynamical Systems:** Discrete and continuous dynamical systems, One and two dimensional maps as discrete dynamical systems, Fixed points, periodic points and stability, Chaos, Lyapunov exponents and chaotic attractors, Differential equations as continuous dynamical systems, Periodic orbits and limit sets, Bifurcations.

### Text/References

1. S. Goldberg: Introduction to difference Equations, Dover, 1986.
2. K.T. Alligood, T.D. Sauer and J.A. Yorke: An Introduction to Dynamical Systems, Springer, 1997.
3. E. Ott: Chaos in Dynamical Systems, Cambridge University Press, 2<sup>nd</sup> edition 2002.
4. S.H. Strogatz: Nonlinear Dynamics and Chaos - With Applications to Physics, Biology, Chemistry and Engineering, Westview Press, 2000.
5. S. Elaydi: An Introduction to Difference Equations, Springer, 1995.
6. W.G. Kelley and A.C. Peterson: Difference Equations - An Introduction with Applications, 2<sup>nd</sup> edition, AP, 2001.

## Unit I

The Communication Channel, The coding problem, Block codes, Hamming metric, Nearest neighbour decoding, Linear codes, Generator and parity check matrices, dual codes, Standard array decoding, Syndrome decoding, Permutation equivalent codes.

## Unit II

Hamming codes, Golay codes, Reed–Muller codes, Codes derived from hadamard matrices. Bounds on codes:  $A_q(n, d)$  and  $B_q(n, d)$ , sphere packing bound, covering radius and perfect codes. Singleton bound and MDS codes, Gilbert lower bound and Varshamov lower bound, Plotkin bound.

## Unit III

Finite fields, cyclotomic cosets and minimal polynomials. Cyclic codes: factoring  $x^n - 1$ , basic theory of cyclic codes, Generator polynomial and check polynomial, minimum distance of cyclic codes.

BCH bound, Encoding decoding of cyclic codes, Hamming and Golay codes as cyclic codes, BCH codes, Reed-Soloman codes, Quadratic residue codes, Graphical codes, Convolutional codes.

**Texts/References**

1. W.C. Huffman and V. Pless: Fundamentals of Error-correcting Codes, Cambridge University Press, 2003.
2. S. Ling and C. Xing: Coding Theory - A First Course, Cambridge University Press, 2004.
3. E. R. Berlekamp: *Algebraic Coding Theory*, Aegean Park Press, 1984.
4. J. H. Van Lint: Introduction to Coding Theory, 3<sup>rd</sup> edition, Springer, 1999.
5. R. Roth: Introduction to Coding Theory, Cambridge University Press, 2006.
6. S. Roman: Introduction to Coding and Information Theory, Springer-Verlag, 1997.

Unit I-Linear Operators, self adjoint operators and compact operators.

Unit II- Eigenvalues, Eigenvectors, Spectrum, spectral theorem, Sturm-Liouville systems, and the Fredholm alternative.

Unit III- Nonlinear operators, variational inequalities, complementarity problems.

**Texts/References**

1. B. Choudhary and S. Nanda: Functional Analysis with Applications, Wiley, 1989.
2. E. Kreyszig: Introductory Functional Analysis with Applications, Wiley, 1978.
3. N. Dunford and J. T. Schwartz: Linear Operators, Part I-III, Wiley, 2009.
4. G. Bachman and L. Narici: Functional analysis, AP, 1966.

**Unit1:** Introduction to Operating Systems, Evolution, Types of OS. Processes: Concept of processes, process scheduling, operations on processes, co-operating processes, interprocess communication. Overview of Threads, benefits of threads, CPU scheduling Criteria, Scheduling Algorithms (FCFS, SRTN, RR), Algorithm evaluation. Process Synchronization, critical section problem, critical region, classical problems of synchronization, semaphores. Deadlocks: Deadlock characterization, Methods to handle deadlocks, deadlock (prevention, avoidance, detection, recovery).

**Unit 2:** Memory Management, logical vs. physical address space, swapping, contiguous memory allocation, paging, segmentation, segmentation with paging. Virtual Memory, demand paging, performance, page replacement, page replacement algorithms (FCFS, LRU), allocation of frames, thrashing, Concept of Cache Memory.

**Unit 3:** File System concepts, access methods, directory structure, file system structure, allocation methods (contiguous, linked and indexed) and free-space management. Disk Management: disk structure, disk scheduling (FCFS, SSTF, SCAN, C-SCAN). Protection and Security.

**Laboratory:** Basic Unix command, Simple shell scripts theory and lab.

#### Text/References

1. A. S. Tanenbaum: Operating System Design and Implementation, 3<sup>rd</sup> edition, Phi Learning, 2009.
2. A. Silberschatz, G. Gagne and P.B. Galvin: Operating System Concepts, Wiley, 2009.
3. D. M. Dhamdhare: Operating Systems - A Concept Based Approach, 3<sup>rd</sup> edition, 2012.
4. W. Stallings: Operating Systems: Internals and Design Principles, 6<sup>th</sup> edition, Pearson Education, 2009.
5. S. Das: Unix Concept and Application, Tata McGraw-Hill, 2006.

### Relational Database Management Systems (RDBMS)

(3-0-1 4)

**Unit 1:** Data and Database Management System, the Database Life Cycle, the Relational Model. ER Model: Entities, Relationship, Attributes, Degree of Relationship connectivity, attributes of a relationship. Concepts of Generalization, Specialization & Aggregation. Concepts of FD. Normalisation: 1NF, 2NF, 3NF & BCNF, lossless join, dependency preservation. Denormalization.

**Unit 2:** Relational Algebra & Calculus. Transforming the Conceptual Data Model to SQL Storage using RAID architecture. B-tree and B<sup>+</sup>-tree Index Files. Measures of Query Cost & overview of query evaluation.

**Unit 3:** Transaction concept, Concurrency Control, Database Recovery.

**Laboratory:** Types of SQL commands: DDL, DML, DQL & DCL. Tables: create, alter, drop. View: creating view, Data query and manipulation with view. Testing for NULL and when not to use NULL. Aggregate Functions: Count(), SUM(), AVG(), MAX(), MIN().

Select Statement, Subqueries, INSERT, UPDATE and DELETE operation. Joins: Natural join, Self join, outer join and Cartesian product. Data security: GRANT and REVOKE.

### **Texts/References**

1. T. J. Teorey et al.: Database Modelling and Design: Logical Design, 4th Edition, Morgan Kaufmann, 2005.
2. A. Silberschatz, H. F. Korth and S. Sudarshan: – Database System Concepts, 6<sup>th</sup> edition, McGraw Hill, 2010.
3. A. Leon, M. Leon: SQL A Complete Reference, McGraw Hill, 1999.

## **Classical Mechanics**

**(3-1-0- 4)**

Integrals of Motion: Ignorable Coordinates, Routhian function. Generalized coordinates, Lagrange's equations, Hamilton's canonical equations, Hamilton's principle and principle of least action, Hamilton Jacobi equation, Poisson and Lagrange's Brackets, Canonical transformation'. Two-dimensional motion of rigid bodies, Euler's dynamical equations for the motion of a rigid body about a fixed point, theory of small oscillations.

### **Text/References:**

1. T. Greenwood: Classical Dynamics, Dover, 1997.
2. H. Goldstein, C.R. Poole and J. Safko: Classical Mechanics, 3<sup>rd</sup> Edition, Pearson India, 2002.
3. E.T. Whittaker: A Treatise on the Analytical Dynamics of Particles and Rigid Bodies: With an Introduction to the Problem of Three Bodies, 4th edition, CUP, 1989.
4. L.D. Landau and E.M. Lifshitz: Mechanics, 3<sup>rd</sup> edition, Butterworth-Heinemann, 1976.
5. H.C. Corben and P. Stehle: Classical Mechanics, 2<sup>nd</sup> edition, Dover Publications, 1994.
6. J.B. Marion and S.T. Thornton: Classical Dynamics of Particles and Systems, 5<sup>th</sup> edition, Cengage Learning, 2003.
7. V.I. Arnold and A. Weinstein: Mathematical Methods of Classical Mechanics, 2<sup>nd</sup> edition, Springer, 1989.

## **Tensor Algebra**

**(3-1-0 4)**

**UNIT-I** Transformation of coordinates, Tensors, Algebra of Tensor, Symmetric and skew-Symmetric tensors, Contraction of Tensor and Quotient law, Riemannian metric, Christoffel Symbol, Covariant derivatives, Intrinsic derivatives and geodesics, Riemann Christoffel Curvature Tensor and its symmetry properties, Bianchi identities and Einstein tensor.

**UNIT-II** Quick Review of the special theory of relativity and general relativity, Einstein's Field equations, Schwarzschild's external solution and isotropic form, Energy-Momentum tensor of a perfect fluid, Schwarzschild's internal solution, Boundary conditions, Energy-Momentum tensor of an electromagnetic field, Einstein-Maxwell equations, Reissner-Nordstrom solution.

### Texts/References

1. C. E. Weatherburn: An Introduction to Riemannian Geometry and the Tensor Calculus, CUP, 2008.
2. H. Stephani et al.: General Relativity: An Introduction to the Theory of Gravitational Field, 2<sup>nd</sup> edition, CUP, 1990.
3. A. S. Eddington: The Mathematical Theory of Relativity, 2<sup>nd</sup> edition, CUP, 2010.
4. J. V. Narlikar: Lectures on General Relativity and Cosmology, Macmillan Press, 1979
5. R. Adler: Introduction to General Relativity, 2<sup>nd</sup> edition, McGraw-Hill, 1975.
6. B. Schutz: A First Course in General Relativity, 2<sup>nd</sup> edition, CUP, 2010.
7. J.K. Goyal and K.P. Gupta: Theory of Relativity, Krishna Prakashan, 1976.

### **Differential Manifold**

**(3-1-0 4)**

Quick review to Curves and Surfaces (at most 5 classes), Derivative of a function from an open subset of  $\mathbb{R}^n$  into  $\mathbb{R}^m$  as a linear transformation. Chain rule. Partial derivatives. Taylor's theorem. Inverse function theorem. Implicit function theorem, Jacobians.

Manifolds, Smooth maps and diffeomorphisms, Tangent Spaces to a manifold, Derivatives of smooths maps, Immersions and submersions, submanifolds, Vector fields, Flows and exponential map, Frobenius theorem, Lie groups and Lie algebras, Homogeneous spaces, Multilinear algebra, Exterior algebra, Tensor fields, Exterior derivative, Lie derivatives. Orientable manifolds, Integration on manifolds, Stokes' theorem, Tangent Bundles and Vector Bundles.

### Texts/References

1. S. Kumaresan: A Course in Differential Geometry and Lie Groups, Hindustan Book Agency, 2002.
2. J. R. Munkres: Analysis on Manifolds, Westview Press, 1997.
3. S. Lang: Introduction to Differentiable Manifold, 2<sup>nd</sup> edition, Springer, 1972.
4. L. Auslander and R. E. Mackenzie: Introduction to Differentiable Manifolds, Dover, 2009.